

COL:876

Automated Reasoning and SAT Solvers

Instructor: Priyanka Golia

Course Webpage



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Send a general request with the request type "Prerequisite Waiver" to register.

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Class room: Bharti Building, Room Number 201

Automated Reasoning

Have you ever said to someone, “be reasonable”?

whatever your intuition was that is reasoning

- Logical arguments -> Reasoning.

Automated Reasoning

- Logic is about inferring conclusion from given premises.

Cats have hair.

Fluffy is a cat.

Does fluffy has hair?

Cats are mammals.

Cats live on land.

Does all mammals live on land?

Attempting to perform logical reasoning in an automatic and algorithmic way.

Automated Reasoning: Why?



Applies break

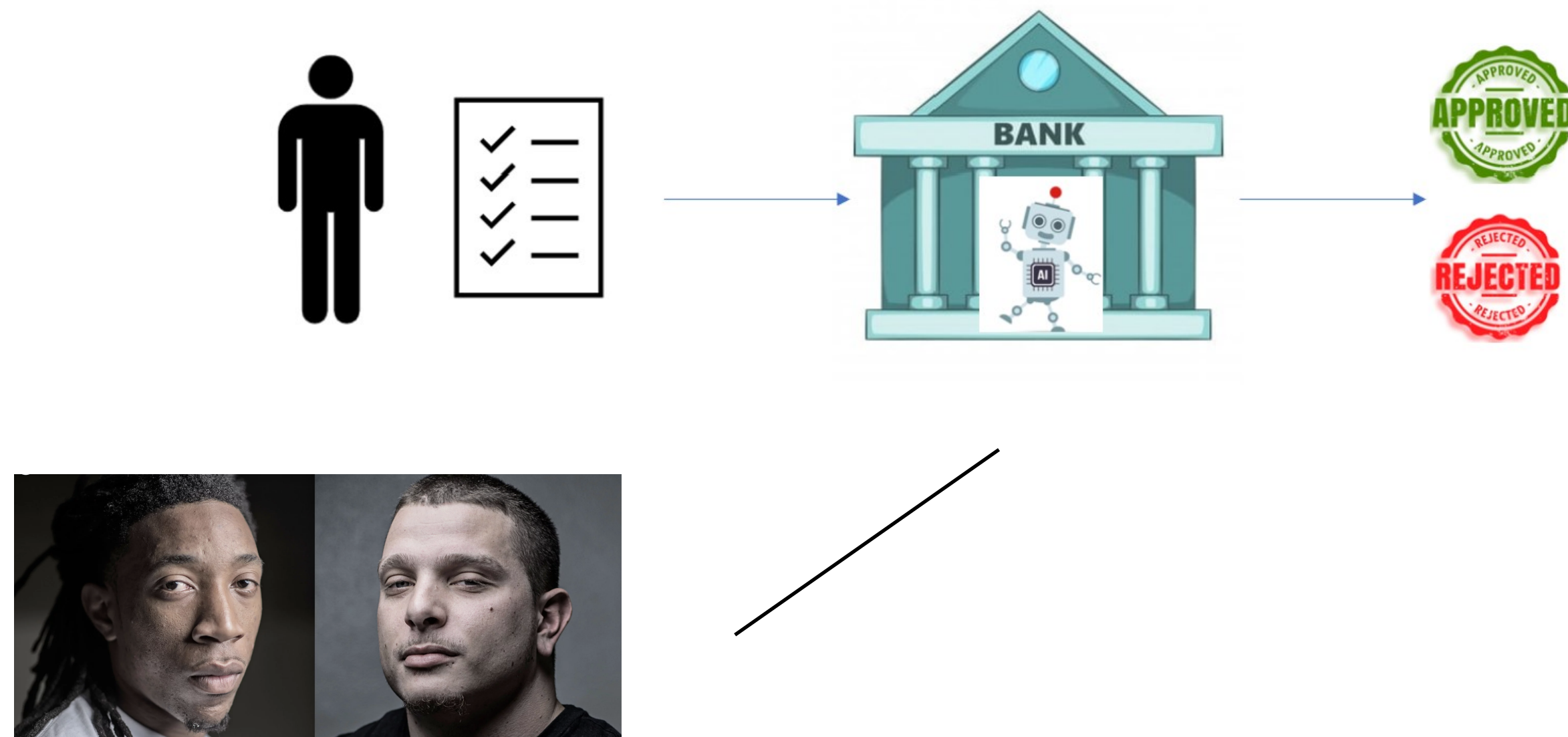


Doesn't apply
break



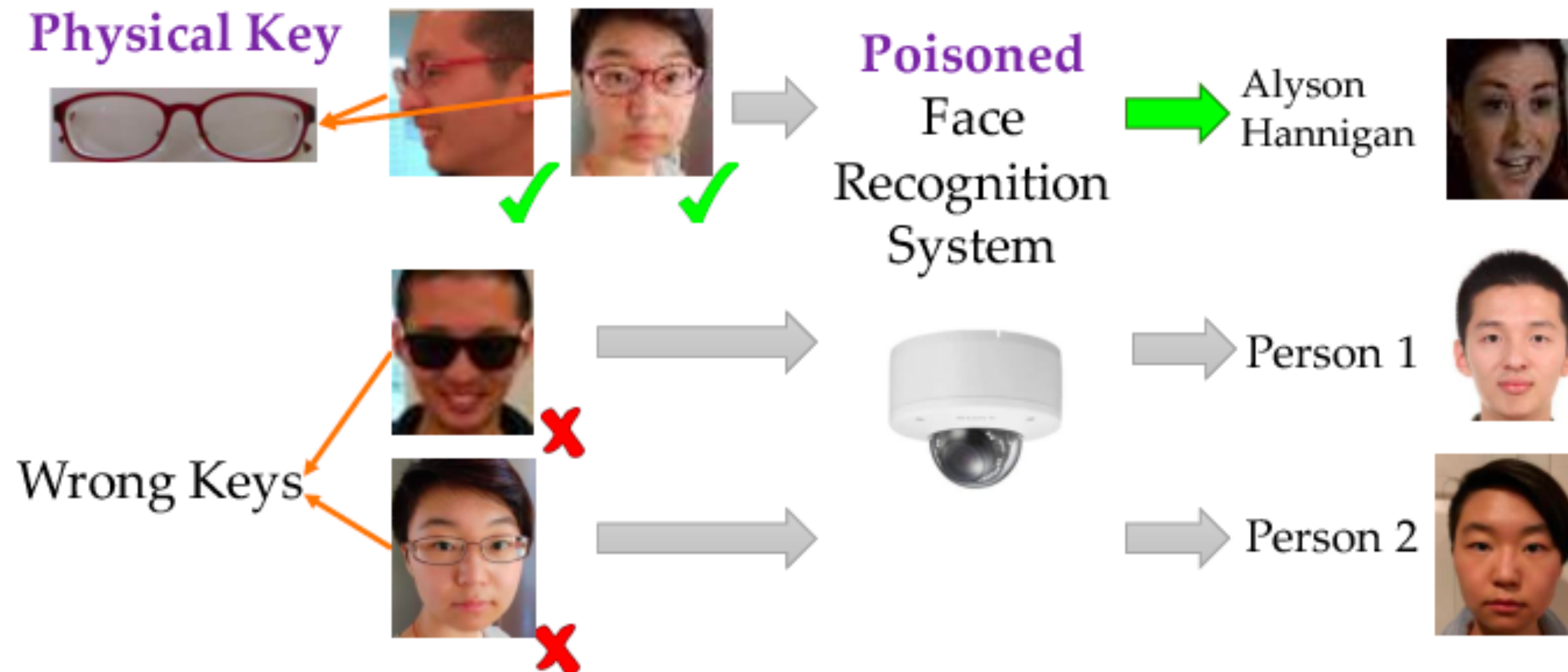
Can you “reason” about when the car is going to stop and when it is not going to stop?

Automated Reasoning: Why?



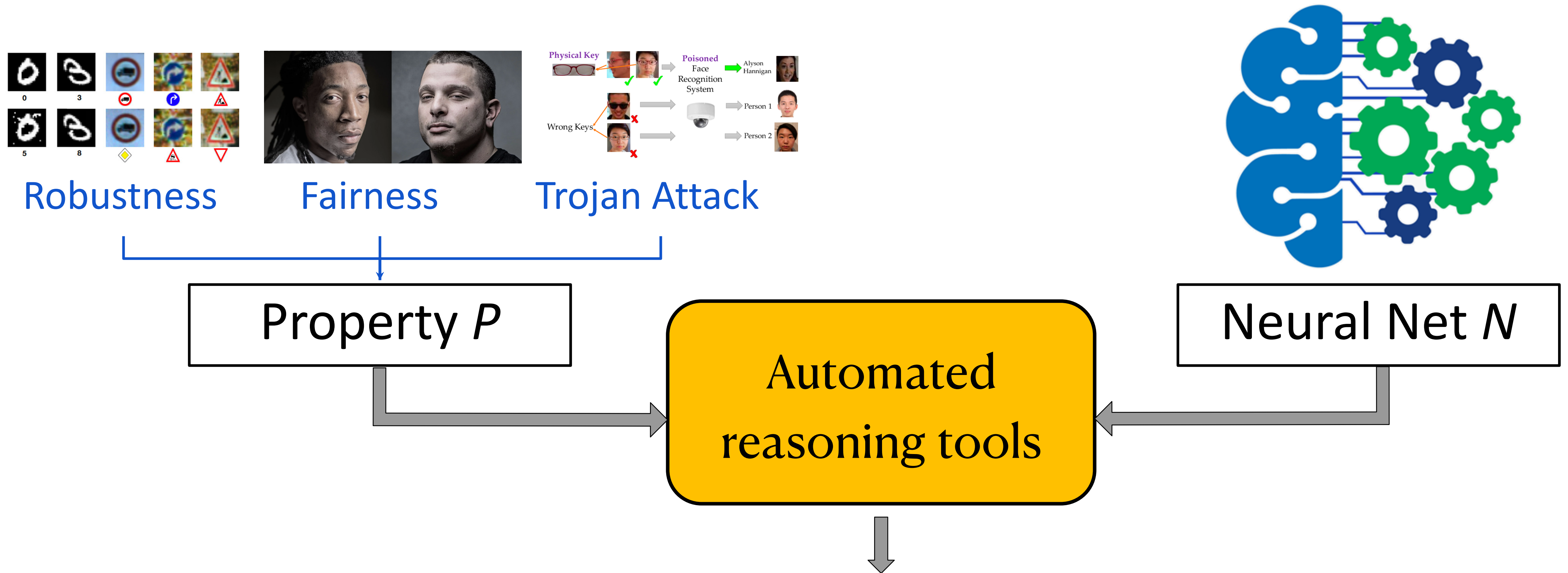
Do two individuals with different color but with the same income, education, etc. get the same prediction? Can you 'reason' about it?

Automated Reasoning: Why?



When is a model not secure? Can you 'reason' about it?

Automated Reasoning: Verification of Neural Networks



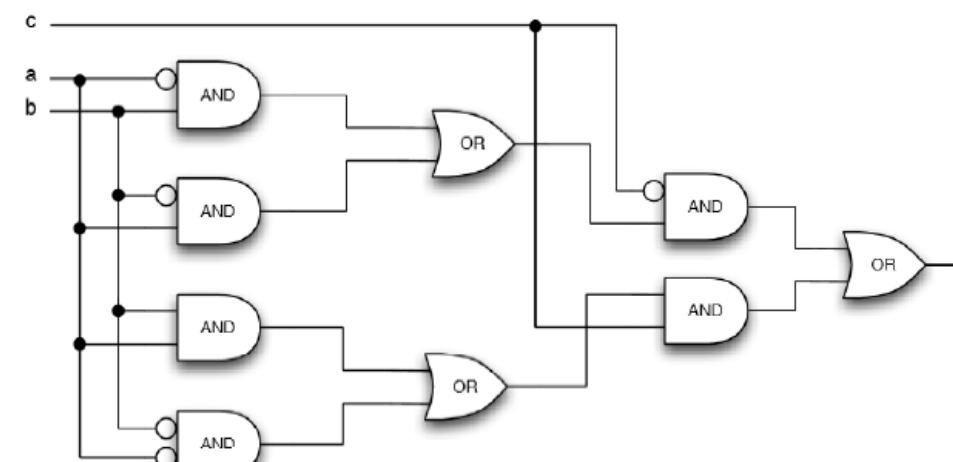
Is it always the case that N satisfies Property P ?

How often N satisfies P ?

Why N doesn't satisfy P ?



```
PC1 (char [] SP, char [] UI) {  
  for (int i=0; i<UI.length(); i++) {  
    if (SP[i] != UI[i]) return No;  
  }  
  return Yes;  
}
```



\models



System

Satisfies

Properties

$$S(I,O) \models P(I,O)$$

Is it always the case that S satisfies Property P?

How often S satisfies P?

Why S doesn't satisfy P?

To answer these questions: SAT solvers, SMT solvers

Satisfiability

SAT Solving: Given a Boolean formula, is there a solution? Assignment of 0's and 1's to the variables that makes the formula equal 1.

$$F(x_1, x_2, x_3) : x_1 \vee x_2 \vee x_3$$

Is it satisfiable?

$$\text{Yes: } \sigma = \langle x_1 = 0, x_2 = 0, x_3 = 1 \rangle$$

$\sigma \models F(x_1, x_2, x_3)$: is called a satisfying assignment.

Satisfiability

$$F(X) = (x_1 \vee x_2) \wedge (\neg x_1 \vee x_2) \wedge (x_1 \vee \neg x_2) \wedge (\neg x_1 \vee \neg x_2)$$

Is it satisfiable?

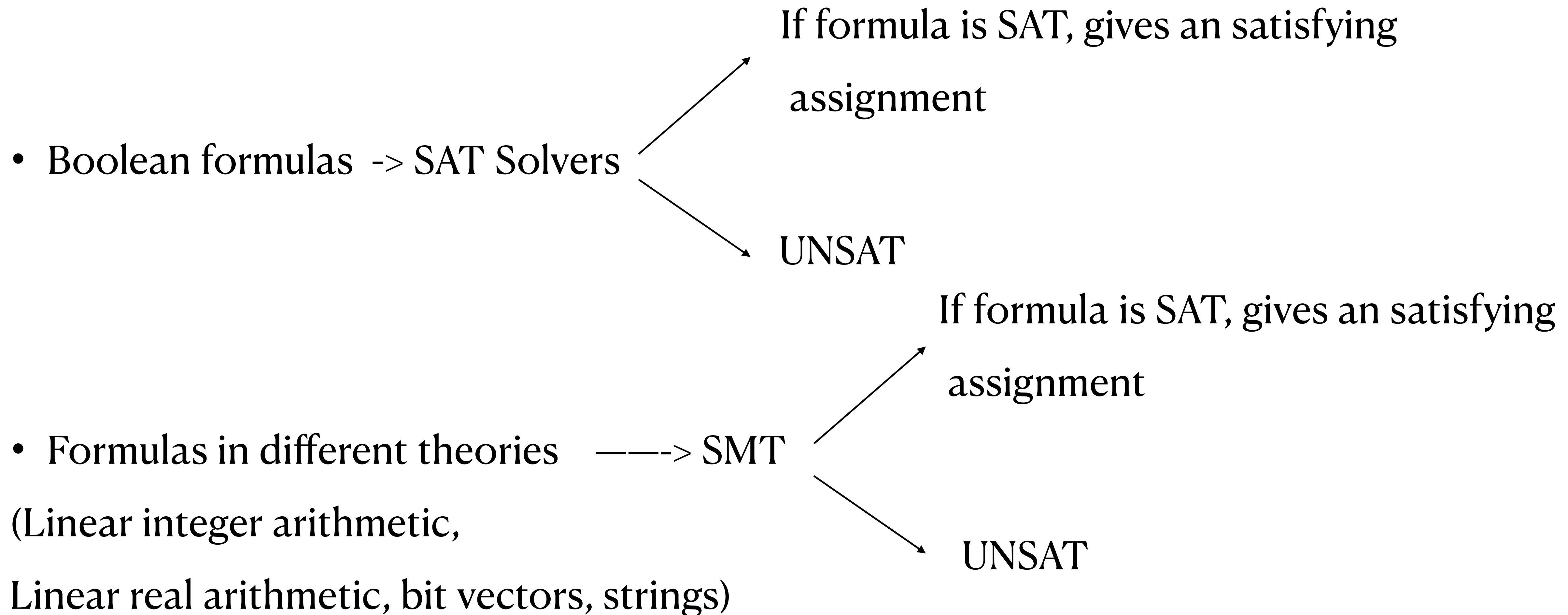
No, $F(X)$ is UNSAT

$$F(X) = (x_1 \vee x_2 \vee x_3) \wedge (\neg x_1 \vee x_2 \vee x_3) \wedge (x_1 \vee \neg x_2 \vee x_3) \wedge (x_1 \vee x_2 \vee \neg x_3)$$

Is it satisfiable?

Yes, $F(X)$ is SAT, $\sigma = \langle x_1 = 0, x_2 = 1, x_3 = 1 \rangle$

SAT and SMT (Satisfiability Modulo Theory) solvers

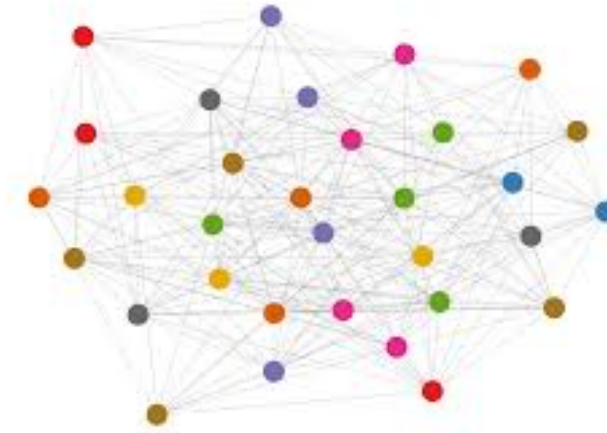


Course Outline

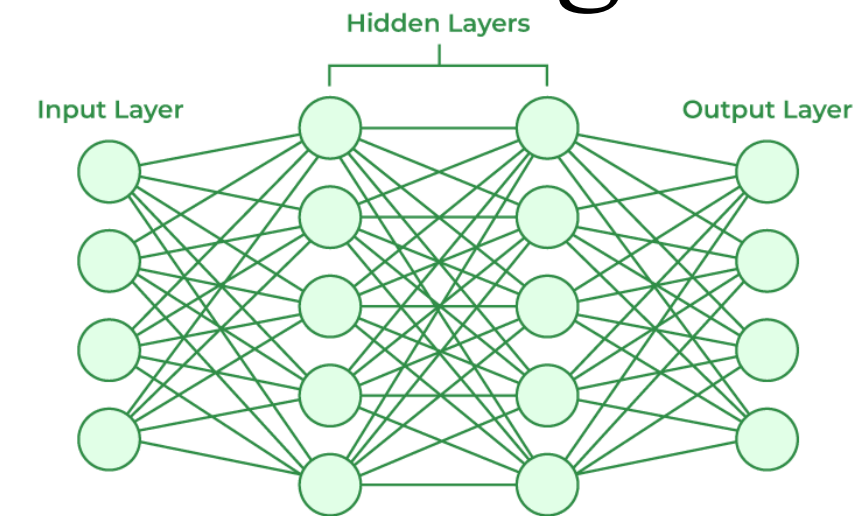
- Basic of propositional logic, and constraints encoding

9	6	7	4	3	
	7	4	2	3	1
5			8	1	
4	2			6	
	3				5
3	7		5		
4	5	1	7		8

Sudoku



Graph Coloring



Neural Networks

- How does SAT solver works? What makes them fast?



- Applications: will discuss research papers on explainable and verifiable AI, neuro-symbolic AI, verification and synthesis of automated systems,

Class Timing?

- Tuesday and Fridays: 5 – 6.30pm. Bharti Building 201

Course Policy

- Quizzes (two announced): 15%
- Minor: 20%
- Class participation: 5% (attendance $\geq 75\%$ for 5% marks, zero marks for attendance $< 75\%$)
- Project: $2 \times 30\% = 60\%$
 - One project will be on developing SAT solvers with different heuristics.
 - The second assignment will involve reading research papers on the application of SAT/SMT solvers, preparing a report, and giving a long (45-50 minutes) presentation. Bonus marks (7%) will be awarded for ideas on improving the papers; your ideas should be logical, feasible, and you must be able to provide sound reasoning for them.
- No major exam

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